

1. Find the breakaway points for  $k>0$  and  $k<0$  and obtain the break in points of them.

$$G(s)H(s) = \frac{K}{s(s+1)(s+2)}$$

2. Plot the root locus diagram for positive values of  $K$  for the solutions of the equation

$$s^4 + 3s^3 + 12s^2 + (k - 16)s + k = 0$$

Find the imaginary roots of equation

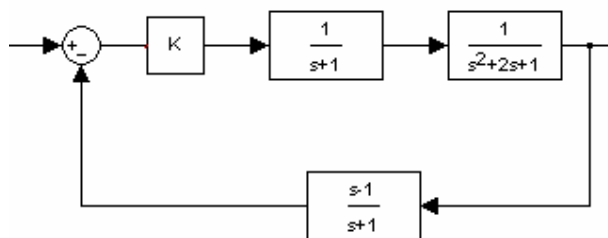
3. Qualitative analysis of the root locus, Plot the

a. root locus diagram for  $G(s) = \frac{K}{s(s+1)}, H(s) = 1$

b. root locus with additional zero:  $G(s) = \frac{K(s+1.5)}{s(s+1)}, H(s) = 1$

c. root locus with additional pole:  $G(s) = \frac{K}{s(s+1)(s+2)}, H(s) = 1$

4. A feedback control system is shown bellow. Draw the root locus for the system and determine the smallest value of gain  $K$  for which a closed-loop pole has a positive real part.



5. Design of PD controller for  $G(s) = \frac{1}{s(s+2)}$  to have :

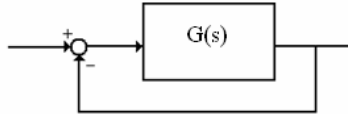
steady state error for ramp input = 0.125

percent overshoot = 16.3

6. For a system that shown in Figure,  $G(s) = \frac{K}{s(s+2)^2}$  design lead controller with a

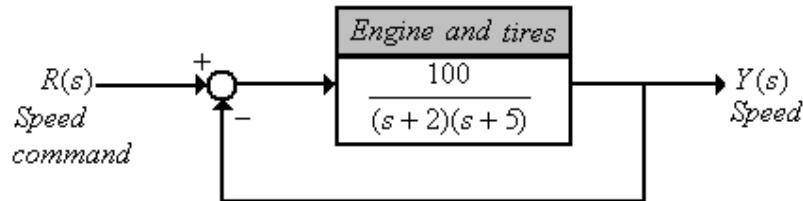
zero in -1, to set rise time of system less than 1 second and percent overshoot less

than 20%. So we want to place dominant poles of system in  $-1 \pm j\sqrt{3}$  and then its  $\xi = 0.5$  and  $\omega_n = 2$



7. The engine, body, and tires of a racing vehicle affect the acceleration and speed attainable. The speed control of the car is represented by the model shown in Figure.

- (a) Calculate the steady-state error of the car to a step command in speed.
- (b) Calculate overshoot of the speed to a step command.



8. A unity negative feedback control system has the unstable plant

$$G(s) = \frac{1}{(s^2 - 1)(s + 5)}$$

. With a PD controller stable the system and set  $\xi = 0.5$  and  $\omega_n = 2$  for its dominant poles.