A Banach algebra without any topological divisor of zero.

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Clearly $\mathcal{C}$ has no topological divisor of zero. In fact $\mathcal{C}$ is the only Banach algebra with this property. (cf. [W. Zelazco, On generalized topological divisors of zero in real m-convex algebras, (1967) 241-244.]).