

A non-primitive C^* -algebra.

$C[0,1]$. In fact if A is a commutative primitive C^* -algebra, then A has a nonzero faithful irreducible representation (H, φ) . So $(\varphi(A))' = \mathcal{C}1$. But $\varphi(A)$ is commutative, so $\varphi(A) \subseteq (\varphi(A))' = \mathcal{C}1$. But $\varphi(A) \neq \{0\}$ so $\varphi(A) = \mathcal{C}1$. Thus $A \simeq \varphi(A) = \mathcal{C}1$.