

A simple C^* -algebra.

$K(H)$ is a simple C^* -algebra. For if I is a nonzero closed bi-ideal of $K(H)$, then it is a closed bi-ideal of $B(H)$, so by [Mur, Th. 2.4.7] $F(H) \subseteq I$, hence $K(H) = \overline{F(H)} \subseteq \bar{I} = I$. Therefore $I = K(H)$.

Ref.

[Mur] G.J. Murphy, C^* -algebras and operator theory, Academic Press, 1990.